Financial Linkages, Portfolio Choice and Systemic Risk

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Motivation

- Financial networks reflect cross-ownership across corporations, short term borrowing and lending among banks, international financial flows and norms of risk sharing.
- They have the potential to smoothen the shocks and uncertainties faced by individual components of the system. But they also create a wedge between ownership and control on the other hand.
- We wish to understand how the empirically observed core-periphery networks mediate this agency problem and we ask: does deeper financial integration reduce volatility and raise welfare? What are the properties of an ideal financial network?

The model

- Two ingredients:
  - *General model of cross-holdings:* Brioschi, Buzzacchi, and Colombo (1989), Eisenberg, and Noe (2001), Fedenia, Hodder, and Triantis (1994), Elliott, Golub abd Jackson (2014).
  - *Separation between ownership and control:* Berle and Means (1932), Fama and Jensen (1983) and Shleifer and Vishny (1989).
- **Contribution:**
  1. Relationship: Network topology, risk taking and welfare
  2. Optimal design of networks

Application of our results

Finance

- **Traditional theory:** More extensive ties are beneficial for individuals (Obstfeld and Rogoff, 1996).
- However, the empirical evidence is mixed. Greater international integration sometimes increases volatility at the individual country level (Kose et al 2009).
- **Our theory:** greater integration leads to greater volatility in returns as well as greater expected returns. Welfare consequences depend on the topology of the network: goes up in homogenous networks but may fall in asymmetric and heterogenous networks(core-periphery network).

Literature

Networks and contagion

- *Networks:* New model of portfolio choice and weighted directed cross ownership.
- Existing work: Allen and Gale (2000) and Gai and Kapadia (2010); recent work Acemoglu, Ozdagler and Talbrezi (2015), Cabrales, Gottardi and Vega-Redondo (2011) and Elliott, Golub and Jackson (2014). Focus on exogenous shocks.
- **Our work:** origin of the shocks – the investments in risky assets – is endogenous. Complementary to complementary to the existing body of work.

The Model

- $N = \{1, 2, ...n\}$ agents (firms, financial institutions, households)
- Agent i with endowment w_i, invests in a project with sure return r and in a risky project i with return $z_i \sim \mathcal{N}(\mu_i, \sigma_i^2)$, $\mu_i > r$.
- Returns of projects are independent.
- Let $\beta_i \in [0, w]$ be agent i's risky investment.
- $\beta = \{\beta_1, ...\beta_n\}$ is the investment profile.

The Financial Network: Ownership

- A network of cross-holdings; $n \times n$ matrix S, with $s_{ii} = 0$, $s_{ij} \geq 0$ and $\sum_{j \in \mathcal{N}} s_{ji} < 1$ for all $i \in \mathcal{N}$.
- Let D be a $n \times n$ diagonal matrix, in which the i^{th} diagonal element is $1 - \sum_{j \in \mathcal{N}} s_{ji}$.
- Define $\Gamma = D[I - S]^{-1}$.

$$\gamma_{ij} = [1 - \sum_{j \in \mathcal{N}} s_{ji}] \left[0 + s_{ij} + \sum_{k} s_{ik} s_{kj} + .. \right].$$

- Interpret γ_{ij} as i's *ownership* of j.

Example: sectors

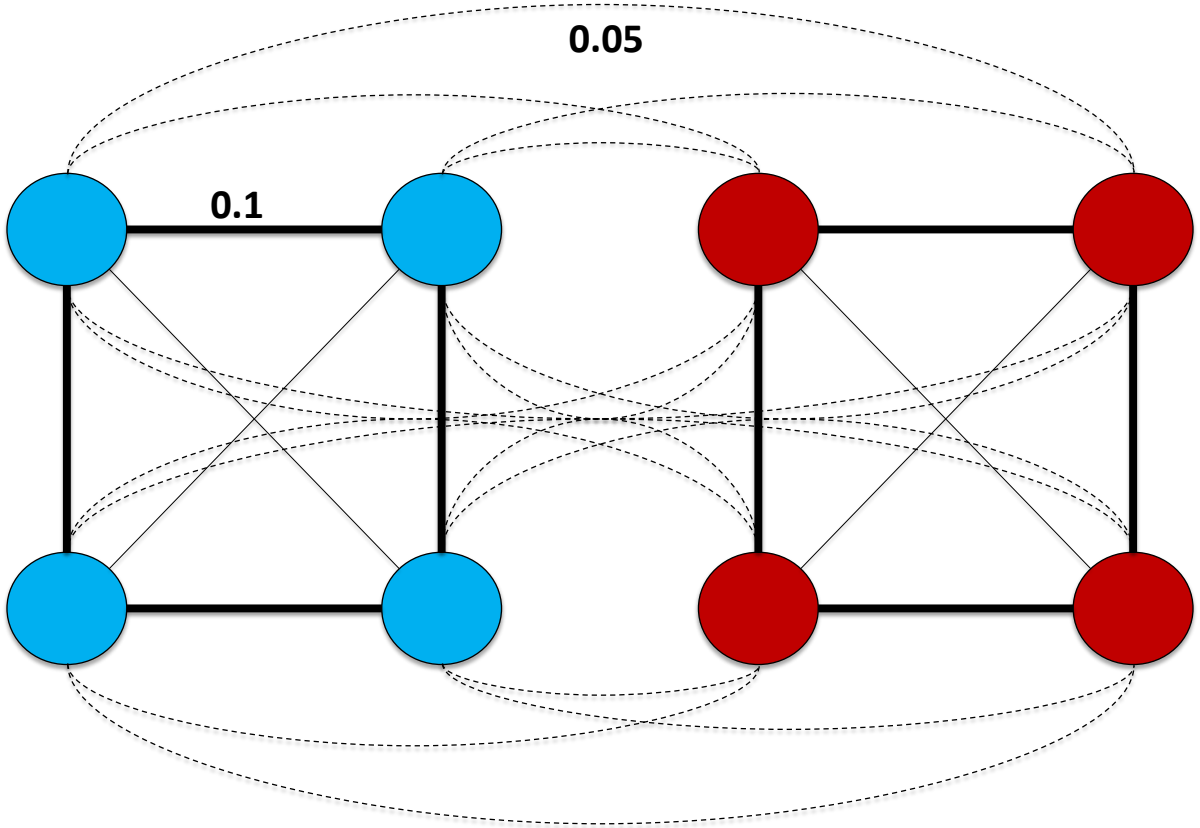


Figure: ownership $\gamma = 0.20$, $\gamma_{\text{across}} = 0.10$, $\gamma_{\text{within}} = 0.133$

Value, Utility and Choice

- The expected returns to individual i

$$W_i = \beta_i z_i + (w_i - \beta_i) r \tag{1}$$

- The economic value of individual i is

$$V_i = \sum_j \gamma_{ij} W_j. \tag{2}$$

- Individuals seek to maximize a mean-variance utility function.

$$U_i(\beta_i, \beta_{-i}) = E[V_i(\beta)] - \frac{\alpha}{2} Var[V_i(\beta)].$$

Systemic Risk

- The network S and choices $\beta^*(S)$ define $\mathcal{V}(S) = \{V_1(S), ..., V_n(S)\}$.
- Two strands of literature:
  1. Supermodular stochastic ordering (SSP). A vector of random variables X dominates another vector Y according to SSP if, and only if, $E[F(X)] > E[F(Y)]$ for all supermodular functions F (Meyer and Strulovici (2012, 2013) and Arlotto and Scarsini (2009)).
  2. Macro finance literature: CoVar and systemic expected shortfall (Brunnermeier (2010), Acharya et al. (2010)). They capture co-movements in the tails of random variables.
- Our definition: S exhibits greater systemic risk than S' if

$$\sum_{i \in \mathcal{N}} \sum_{j \in \mathcal{N} \setminus \{i\}} Cov(V_i(S), V_j(S)) > \sum_{i \in \mathcal{N}} \sum_{j \in \mathcal{N} \setminus \{i\}} Cov(V_i(S'), V_j(S'))$$

Portfolio Choice in Networks

- We begin by characterizing optimal agent investments.
- Observe that cross partial derivatives are zero. So:

$$\beta_i^* = \arg \max_{\beta_i \in [0, w_i]} \gamma_{ii}[w_i r + \beta_i(\mu_i - r)] - \frac{\alpha}{2}\gamma_{ii}^2 \beta_i^2 \sigma_i^2.$$

- If agent i has no cross-holdings then $\gamma_{ii} = 1$ and:

$$\hat{\beta}_i = \frac{\mu_i - r}{\alpha \sigma_i^2}.$$

- $\hat{\beta}_i$ is agent i's *autarchy* investment.

Optimal Portfolio Choice

Proposition

Optimal investment of individual i is:

$$\beta_i^* = \min\left\{ w_i, \frac{\hat{\beta}_i}{\gamma_{ii}} \right\}. \tag{3}$$

- Remark: Investment in risky asset is inversely related to self ownership.
- Agency problem: individual i optimizes the mean-variance utility of $\gamma_{ii} W_i$, not of W_i.

Mean, variance and correlations

- Expected value and variance for individual are:

$$E[V_i] = r\sum_{j\in\mathcal{N}}\gamma_{ij}w_j + \sum_{j\in\mathcal{N}}\hat{\beta}_j(\mu_j - r)\frac{\gamma_{ij}}{\gamma_{jj}} \quad Var[V_i] = \sum_{j\in\mathcal{N}}\hat{\beta}_j^2\sigma_j^2\left(\frac{\gamma_{ij}}{\gamma_{jj}}\right)^2,$$

  - More ownership of individuals with low self-ownership: greater expected value and variance.
- The covariance between V_i and V_j is:

$$Cov(V_i, V_j) = \sum_{l\in\mathcal{N}}\hat{\beta}_l^2\sigma_l^2\frac{\gamma_{il}\gamma_{jl}}{\gamma_{ll}^2}.$$

  - **Systemic risk:** covariance between V_i and V_j is higher with common ownership of low self-ownership individuals.

Systemic Risk across Sectors

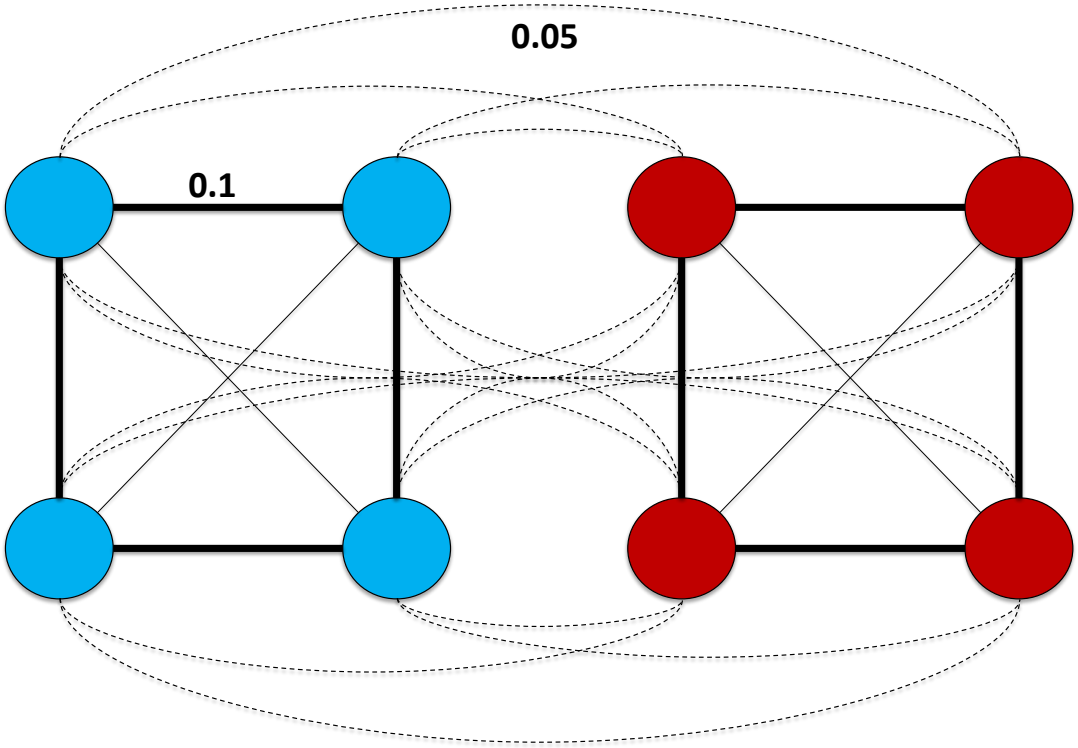
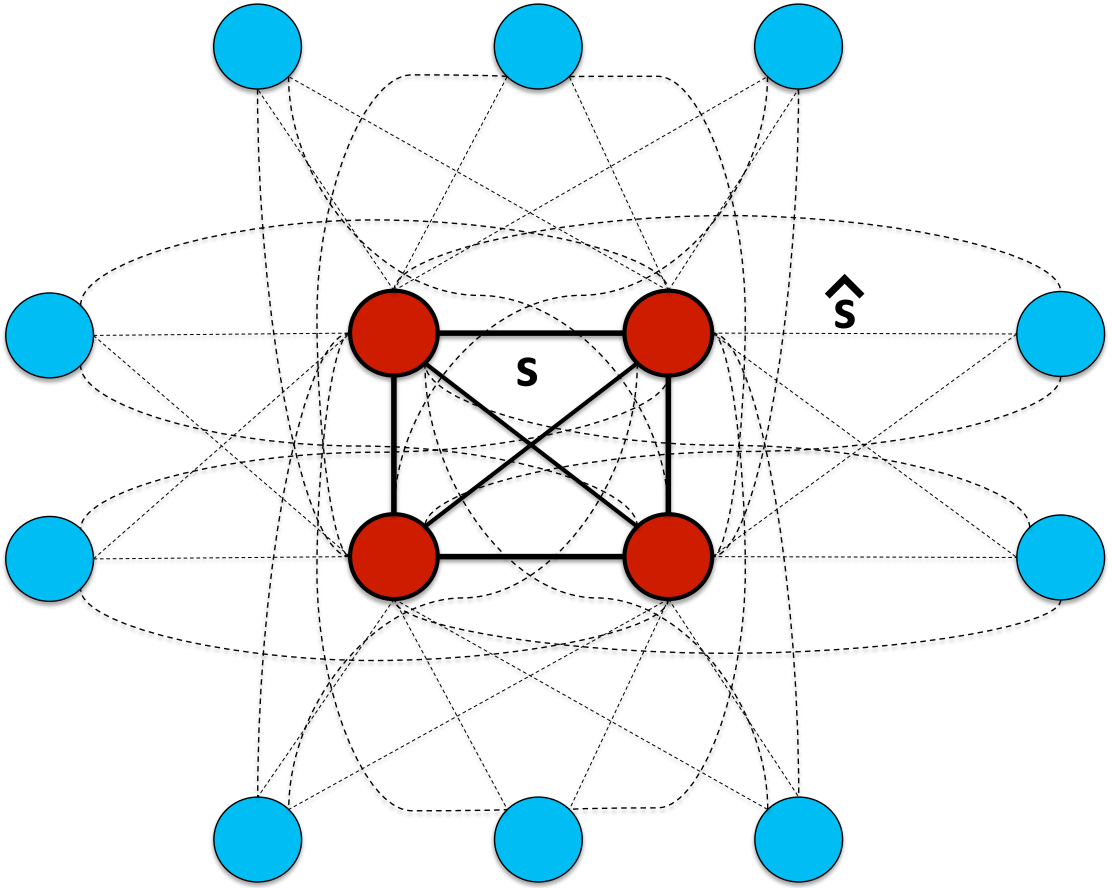


Figure: β_i=0.32; correlation within 0.48; correlation across 0.41

Core-periphery Network: motivation

- Financial networks exhibit a core-periphery structure.
- Inter-bank networks: Martinez-Jaramillo et al (2014), Soramaki et al. (2007), van Lelyveld and Veld (2012) and Langfield, Liu and Ota (2014).
- Ownership of transnational corporations: Vitali et al. (2011). They report that transnational corporations form a giant bow-tie structure and that a large portion of control flows to a small tightly-knit core of financial institutions.
- International financial flows: McKinsey Global Institute (2014). This network has a core-periphery structure, with the core constituted of United States and Western Europe and the rest of the world comprising the periphery (mainly having links with the core countries).

Core-periphery Network



Core-periphery network: description

- There are n_p peripheral agents and n_c central agents, $n_p + n_c = n$; i_c and i_p refer to the (generic) central and peripheral agent.
- A link between two central agents has strength $s_{i_c j_c} = s$, and a link between a central and a peripheral agent $s_{i_c i_p} = s_{i_p i_c} = \hat{s}$, and there are no other links.

Ownership Patterns

- Self-ownership of a central node i_c and a peripheral node are, respectively,

$$\gamma_{i_c,i_c} = \frac{[1-(n_c-1)s-n_p\hat{s}][1-(n_c-2)s-n_cn_p\hat{s}^2+n_p\hat{s}^2]}{(s+1)[1-s(n_c-1)-n_cn_p\hat{s}^2]},$$

$$\gamma_{i_p,i_p} = \frac{[1-n_c\hat{s}][1-(n_c-1)s-n_c\hat{s}^2(n_p-1)]}{1-s(n_c-1)-n_cn_p\hat{s}^2}.$$

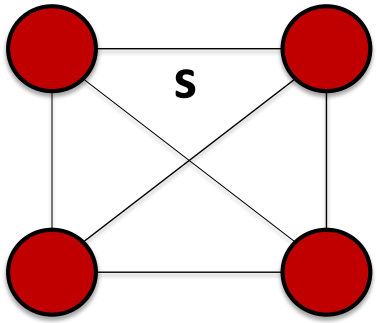
The Complete Network

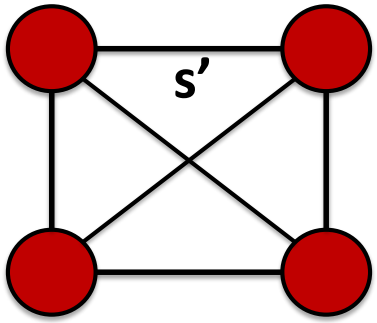
- Every (ordered) pair of agents has a directed link of strength s.
- The ownership matrix Γ in a complete network is

$$\gamma_{ij} = \frac{s}{s+1} \quad \text{and} \quad \gamma_{ii} = 1 - (n-1)\gamma_{ij}.$$

- Greater s lowers self-ownership: all agents raise their risky investments.
- Expected value $E[V_i]$ and variance $Var[V_i]$ increase in s.
- Expected utility of each agent is increasing in s.
- Systemic risk in a complete network is also increasing and convex in strength of connection.

Complete Network





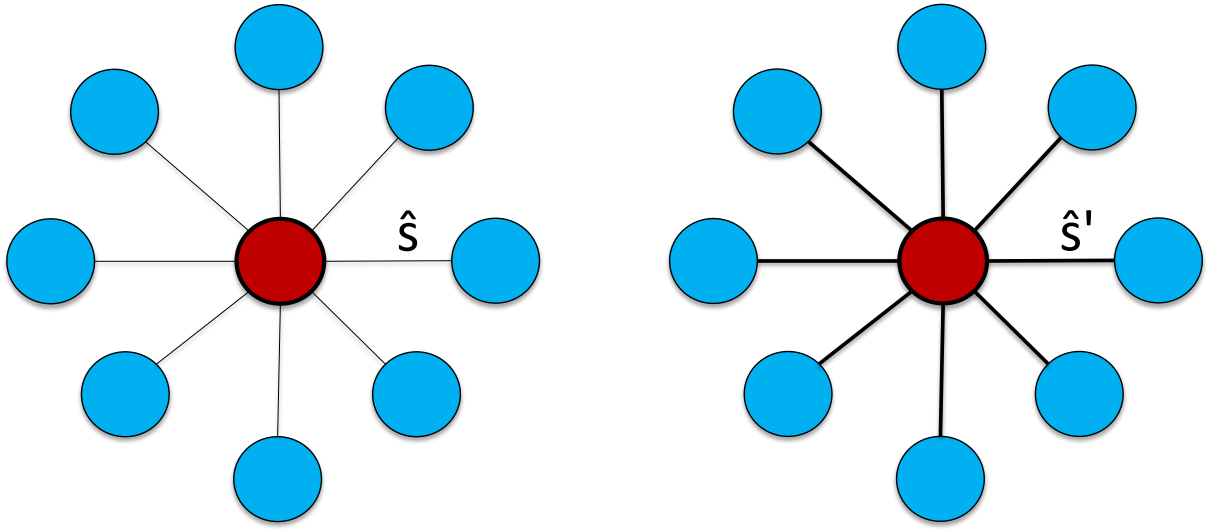
The Star Network

- Set $n_c = 1$ in core-periphery network to get self-ownerships:

$$\gamma_{i_c i_c} = \frac{1 - n_p \hat{s}}{1 - n_p \hat{s}^2} \quad \text{and} \quad \gamma_{i_p i_p} = \frac{[1 - \hat{s}][1 - \hat{s}^2(n_p - 1)]}{1 - n_p \hat{s}^2}.$$

- It is true that $\gamma_{i_c i_c} < \gamma_{i_p i_p}$
- So central agent makes larger investments in the risky asset.

Star Network



The Star Network

- We can deduce that the cross-ownerships are, respectively:

$$\gamma_{i_c,j_p} = \frac{[1 - n_p\hat{s}]\hat{s}}{1 - n_p\hat{s}^2}, \ \gamma_{j_p,i_c} = \frac{[1 - \hat{s}]\hat{s}}{1 - n_p\hat{s}^2}, \ \gamma_{i_p,j_p} = \frac{[1 - \hat{s}]\hat{s}^2}{1 - n_p\hat{s}^2}.$$

- Interesting patterns: for small $\hat{s}$, the central player has higher mean and variance than the peripheral players; the converse holds for large $\hat{s}$.

Intuition

- Small $\hat{s}$: everyone has high self-ownership, own investment is what matters more for the mean and variance of value. Central agent invests more in the risky asset so he obtains higher returns and variance.
- $\hat{s}$ high: the central player has very little self-ownership and ownership of peripheral players. In contrast, the peripheral players have positive and large ownership of the central player. Peripheral players absorb the large risky investments that the central player undertakes.

Welfare

- $\hat{s}$ low: the utility of the central player is higher than the utility of the peripheral players because the center has a higher mean than the peripheral players and the cost of the variance is low, as each agent invests moderately in the risky asset.
- $\hat{s}$ is high: the central player is better off again. In this case, he has a lower mean than the peripheral players, who, however, face very high variance. For intermediate values of $\hat{s}$, the peripheral players may be better off than the center.

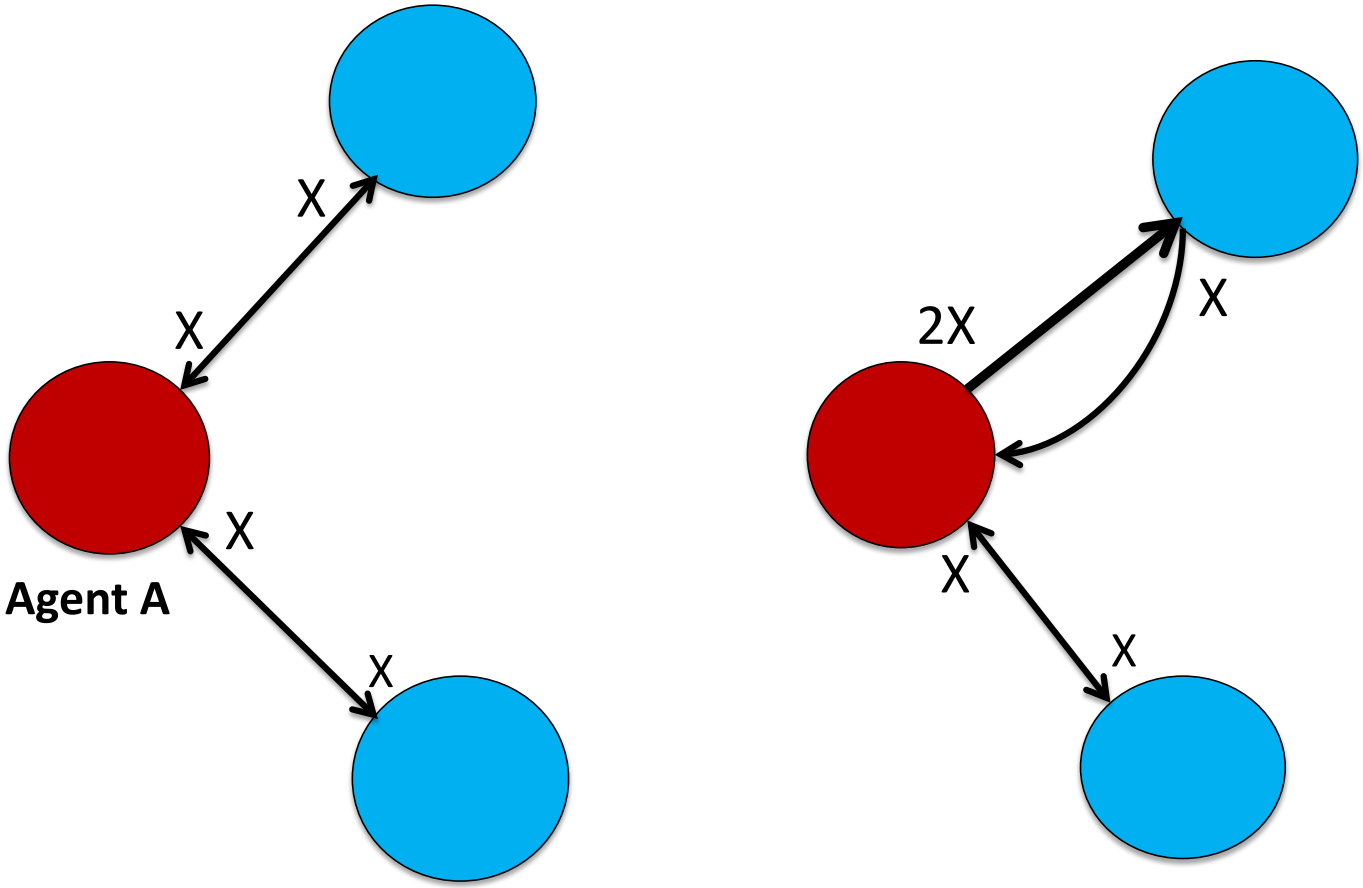
Integration and Diversification

- Financial interconnections have deepened over last 3 decades. Kose et al (2006), Lane and Milesi-Ferretti (2003).
- **Traditional argument**
  - Individuals invest in risky assets that have independent returns: deeper or more extensive linkages should lower variance of earnings. Since individuals are risk averse this raises overall utility.
- **Our result:**
  - Greater linkages encourage more risk taking. Improve welfare in symmetric networks but lower welfare in asymmetric networks such as a core-periphery network.

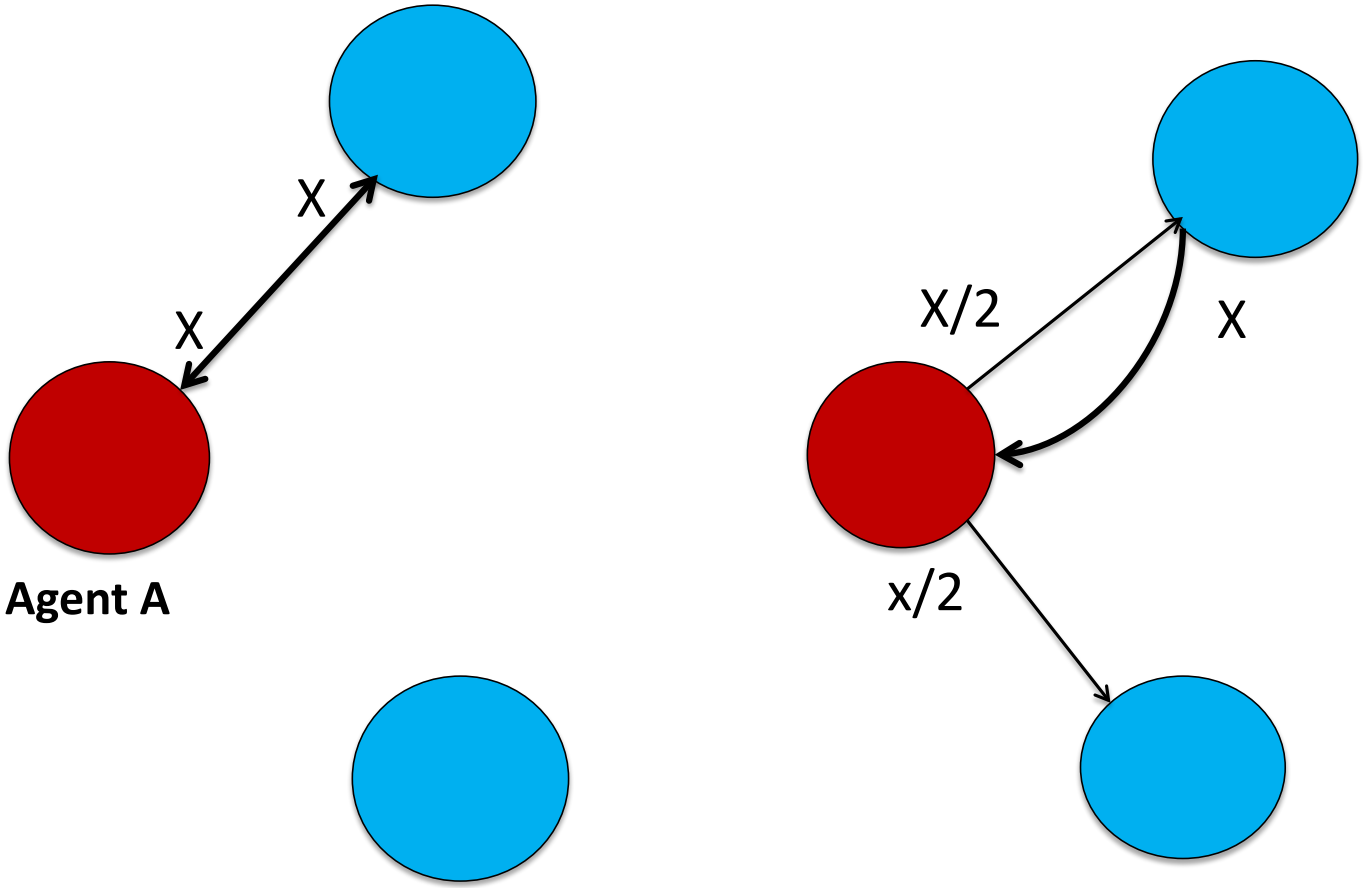
Integration and Diversification

- For a vector $s_i = \{s_{i1}, ..., s_{in}\}$ define the variance of s_i as $\sigma^2_{s_i} = \sum_j (s_{ij} - \eta_i^{out}/(n-1))^2$.
- **Integration** All links are stronger, some strictly so.
- **Diversification** Variance of out-going links is smaller for every node.

Integration



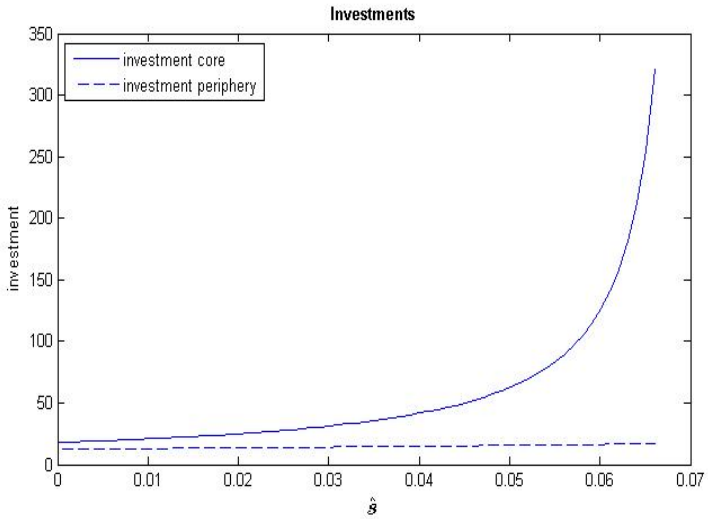
Diversification

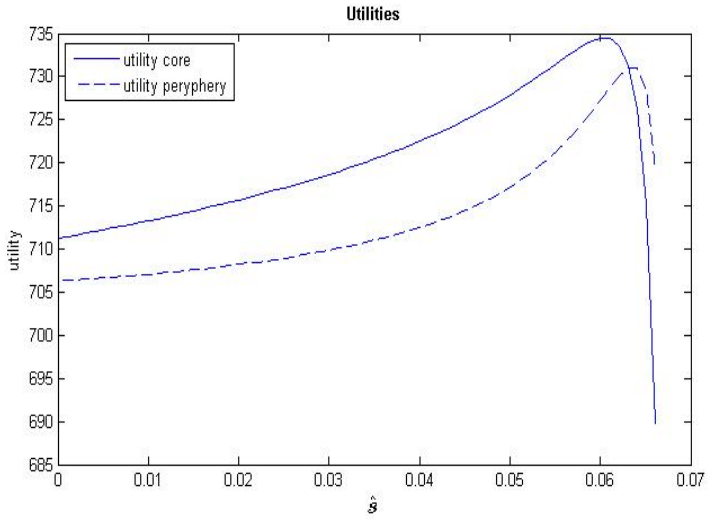


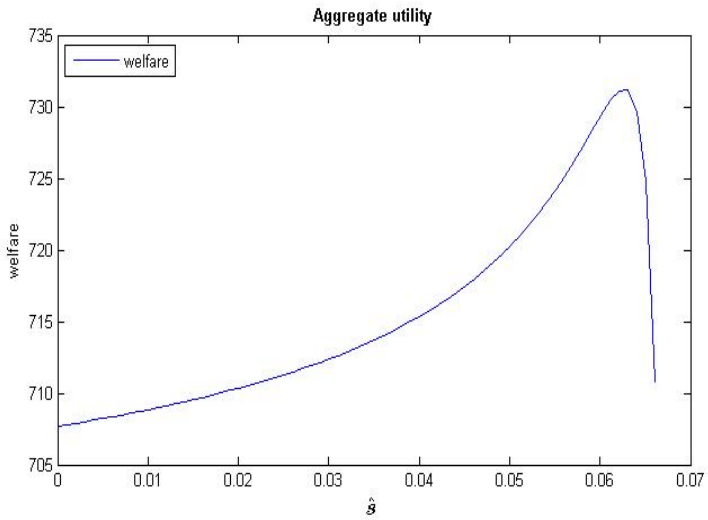
Thought experiment: changes in core-periphery network

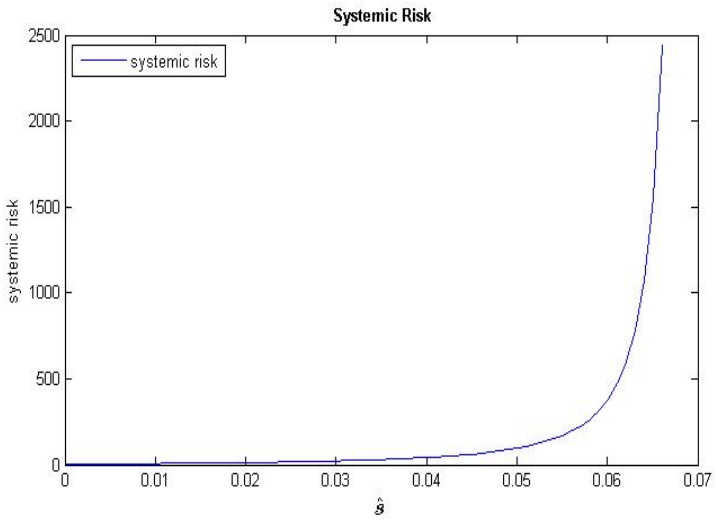
- International Flows: links between periphery and core strengthened over the last three decades, McKinsey Global Institute (2014)
- We change strength of ties in our network and study effects
- Example: $n_c = 4$, $n_p = 10$, $\sigma = 0.4$, $\alpha = 0.5$, $\mu = 2$, $r = 1$, $w = 700$, $s = 0.1$,
- Vary strength of tie: $\hat{s} = \{0...0.065\}$.

Integration in Core-periphery Network









Normative analysis

- What is the welfare maximizing investment for a given network?
- How does it differ from what individuals do: what are the externalities?
- what is the optimal design of financial networks?

Welfare Maximizing Investments

- We consider the following planner function

$$W = \sum_i E[V_i] - \frac{\alpha}{2} Var[V_i] - \frac{\phi}{2} \sum_i \sum_{j \neq i} Cov[V_i, V_j]$$

- When $\phi = 0$ the planner is utilitarian;

- When $\phi = \alpha$ the planner has mean-variance preferences over aggregate returns $V = \sum_i V_i$.

- When ϕ increases from 0 to α the planner becomes more and more averse to systemic risk.

Efficient Investments and externalities

Proposition

The optimal investment of the planner in risky project $i = 1, .., n$ is given by

$$\beta_i^P = \max \left\{ w, \hat{\beta}_i \frac{\alpha}{\phi + (\alpha - \phi) \sum_{j \in \mathcal{N}} \gamma_{ji}^2} \right\}.$$

- Whether individuals take more or less risk: γ_{ii} vs $\sum_{j \in \mathcal{N}} \gamma_{ji}^2$.
- In dispersed networks individuals will invest too little in risky asset
- In networks with concentrated ownerships, reverse is true.

The Optimal Network

Proposition

Consider interior solutions.

- *The first best network design is the complete network with maximum link strength* $s_{ij} = 1/(n-1)$ *for all* $i \neq j$.
- *The second best network design is the complete network with link strength*

$$s_{ij} = \frac{1}{n-1}\frac{\alpha - \phi}{\alpha}, \text{ for all } i \neq j.$$

First best: intuitions

- We first derive the optimal Γ, and then we derive the network S that induces the optimal Γ.
- Homogeneous networks dominate heterogeneous networks: this is because agents are risk-averse, and concentrated and unequal ownership exacerbates the costs of variance.
- This leads to a preference for homogeneous networks: networks where, for every i, $\gamma_{ji} = \gamma_{j'i}$ for all $j, j' \neq i$.
- In the first-best, within homogeneous networks, stronger links are better, as they allow for greater smoothing of shocks, and this is welfare-improving due to agents' risk aversion.

Second best: Intuitions

- Within homogeneous network, the designer has to choose between networks in which agents have high self-ownership (and, therefore, make large investments in the risky asset) *versus* low self-ownership (when they take little risk).
- When the social planner is utilitarian, $\phi = 0$, the optimal network is invariant: $s_{ij} = 1/n - 1$ for all i, j both in the first-best and the second-best case.
- If social planner cares about correlation across agents, then the larger the weight placed on systemic risk, the greater the aversion to correlations in agents' values. second best network is less integrated than the optimal network in the first-best scenario.

Discussion: Ownership and control

- Suppose that γ_{ij} signifies that agent i has control over γ_{ij} fraction of agent j's initial endowment w_j. So $\gamma_{ij} w_j$ is a transfer from j to i that occurs before shocks are realized. Therefore, Γ redefines the agents' initial endowments. No network effects, due to absence of income effects.
- Control is 'local': agent i can invest $w\gamma_{ij}$ in the risk-free asset and in the risky project of agent j. Individually optimal investment levels are independent of network, and choices mimic those of a central planner with mean-variance preferences over aggregate returns $V = \sum_i V_i$.

Discussion: Endogenous networks

- Agents simultaneously demand shares of other firms, supply shares of their own firm, and decide how much risk to take.
- An equilibrium is a network Γ, a price vector $p = \{p_1, ..., p_n\}$ that specifies the price p_i of each share of i, and a profile of investment β, such that each agent's decision is optimal, agents' expectations are rational, and the price clears the market.
- There always exists equilibrium that replicates the outcome of an utilitarian social planner who optimally designs the network and chooses agents' investments.
- Agents' heterogeneity – endowment and in assets – translates into different investment decisions and different prices, but the equilibrium network is always symmetric.
- Frictions in link formation necessary for asymmetric networks.

Discussion: Correlated returns

- In basic model, any form of correlation across agents' economic value is driven by the architecture of the cross-holdings network. The assumption that projects are uncorrelated allows us to isolate the effects of cross-holdings on risk-taking behavior and aggregate outcomes.
- We extend the model to allow for arbitrary correlations across assets.
- We show existence and derive sufficient conditions for uniqueness of an interior equilibrium.
- We then show, via examples, that asymmetric networks may lead to over-investment in risky assets, as in the case of uncorrelated projects.

Summary

- Financial networks reflect cross-ownership across corporations, short term borrowing and lending among banks, inter-national financial flows and norms of risk sharing.
- Financial linkages smoothen the shocks and uncertainties faced by individual components, but they also give rise to an agency problem: there is a wedge between ownership and control.
- We develop a framework of endogenous risk taking by decision makers connected via financial obligations. It formalizes a basic agency problem: decision makers do not internalize entirely the consequence of risk taking.

Summary

- The standard argument on benefits of pooling risk is valid when the network is homogenous. When the ownership of some agents is concentrated, the agency problem becomes salient. Greater integration and diversification may lead to excessive risk taking and volatility; result in lower welfare.
- Optimal networks are homogenous and dense; strength of ties falling in the importance of systemic risk.